

# Health and Inequality

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Work in Progress

# Introduction

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*Marmot et al (L 1991); Smith (JEP 1999); Bohacek, Bueren, Crespo, Mira, Pijoan-Mas (2017)*
- ▷ We want to *compare* and *relate* **inequality in health outcomes** to pure **economic inequality**.

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  - a/ Health-related preferences
  - b/ Health-improving technology with medical expenditures



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  2. Ask what different groups would do if their resources were different and how much does welfare change.

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    - Adds more realistic features
- ▷ Part (3) still preliminary

# Welfare Comparison: Compensated Variation

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1. Under the same preferences  $u(c)$ , then to make them equally happy, we have to set  $u(\bar{c}_d) = u(c_c)$ , i.e. to give  $\frac{\bar{c}_d}{c_c} - 1$  extra consumption to the  $d$  group.

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2. If they have different longevities, then we have to use a  $u$  function that includes consumption and the value of expected longevity  $\ell$ :  $u(c, \ell)$ . Then the compensated variation be the amount  $\frac{\bar{c}_d}{c_c} - 1$  that solves

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4. If we estimate preferences and health maintenance technology when compensating people, they would **alter** their health and longevity in ways we could calculate.

## Stylized Model: The construction of $u$

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6. Let health  $h \in \{h_g, h_b\}$

$$V^e(a, h) = \max_{x, c, a_{h'}} \left\{ u(c, h) + \beta \gamma_h \sum_{h'} \Gamma_{hh'}^e(x) V^e(a_{h'}, h') \right\}$$
$$\text{s.t. } x + c + \gamma_h \sum_{h'} q_{hh'}^e a_{h'} = a(1 + r)$$

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- Standard Complete Market result (Euler equation for  $c$ ):

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- Optimal health investment (Euler equation for  $x$ ):

$$u_c(c_h, h) = \beta \gamma_h \frac{\partial \Gamma_{hh_g}^e(x)}{\partial x} \left( V^e(a'_{h_g}, h_g) - V^e(a'_{h_b}, h_b) \right)$$

- The attained value in each health state is given by

$$\begin{pmatrix} V_g^e \\ V_b^e \end{pmatrix} = A^e \begin{pmatrix} \alpha_g + \chi_g \log c_g^e \\ \alpha_b + \chi_b \log \frac{\chi_b}{\chi_g} c_g^e \end{pmatrix}$$

where 
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**Data**

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- Survival functions (by age, health)

▷ Obtain the objects  $\mu_h^e$ ,  $\Gamma_{hh'}^e(x^*)$ ,  $\gamma_h$

### 2. PSID (1999+) gives

- Non-durable consumption (by age, health, and education type)
- Out of Pocket medical expenditures (by age, health, and education type)

▷ Obtain health modifier of marginal utility  $\chi_h$  ( $\chi_g = 1$ ,  $\chi_b = 0.85$ )

▷ Obtain health technology parameters  $\Lambda^e$

### 3. Standard data in clinical analysis

- Outside estimates of the value of a statistical life (VSL)
- Health Related Quality of Life (HRQL) scoring data from HRS

▷ Obtain  $\alpha_g$ ,  $\alpha_b$

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- Therefore,

$$\frac{u(c_g^e, h_g)}{u(c_b^e, h_b)} = \frac{\alpha_g + \chi_g \log c_g^e}{\alpha_b + \chi_b \log c_b^e} = \frac{0.85}{0.60}$$

## Results without Endogenous Health

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- Our answer

*By revealed preference, it must be that out-of-pocket health spending is not too useful in improving health after age 50*

# Results with Endogenous Health

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- This adds 8 parameters:  $\nu_g, \nu_b, \lambda_{1,g}, \lambda_{1,b}, \lambda_{0,g}^c, \lambda_{0,b}^c, \lambda_{0,g}^d, \lambda_{0,b}^d$

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2. The 4 observed health transitions yield the  $\lambda_{0,h}^e$  for  $e$  and  $h \in \{g, b\}$ .

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  - This is because of low ratio of medical to non-medical expenditure (0.18)

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Panel A: Health Transition Parameters

	$\Gamma_{hg}$	$\lambda_{0h}^e$	$\lambda_{1h}$	$\nu_h$
Good health				
College	0.951	0.935	$3.5 \times 10^{-5}$	0.35
Dropouts	0.895	0.884		
Bad health				
College	0.386	0.367	$1.6 \times 10^{-5}$	0.25
Dropouts	0.125	0.114		

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Panel B: Decomposition of the Life Expectancy Gradient

	Full model	$\mu^c$	$x^c$	$\lambda_{0h}^c$
Life expectancy	5.6	0.7	0.3	4.8
Healthy life expectancy	13.2	1.8	0.7	11.5

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# WELFARE DIFFERENCES WITH ENDOGENOUS HEALTH

## Welfare of different types

	CG-HSG	CG-HSD
Compensated variations ( $1 + \Delta_{(x+c)}$ )		
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Endogenous health choices	<b>2.26</b>	<b>6.86</b>

- This is still a very large difference.

# Quantitative Model

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  - Distribution:  $\log \epsilon \sim N\left(-\frac{1}{2}\sigma_\epsilon^2, \sigma_\epsilon^2\right)$

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## THE BELLMAN EQUATION: THE RETIREE VERSION

- The individual state is given by  $\omega = (e, i, h, a) \in E \times I \times H \times A \equiv \Omega$ .
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- Health investments at each state  $\eta$ :

$$R \sum_{h'} \int_{\epsilon} \Gamma^{ei}[h' | h, \eta, x(\omega, \eta)\epsilon] u_c^{i+1}[h', c(\omega, \eta, h', \epsilon)] f(d\epsilon) =$$
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# Estimation

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    - Need to recover posterior probability of  $\eta_j$  from observed health spending  $\tilde{x}_j$

# Preliminary Estimates: Preferences

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- We use the sample average for all individuals  $j$  of the same type  $\omega$  as a proxy for the expectation over  $\eta$ ,  $h'$ , and  $\epsilon$

$$\beta^e R \tilde{\gamma}_h^i \frac{1}{N_\omega} \sum_j \mathbf{1}_{\omega_j=\omega} \frac{\chi_{h_j'}^{i+1}}{\chi_h^i} \left( \frac{c_j'}{c_j} \right)^{-\sigma} = 1 \quad \forall \omega \in \tilde{\Omega}$$

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- Use consumption growth from PSID by education, health, wealth, age

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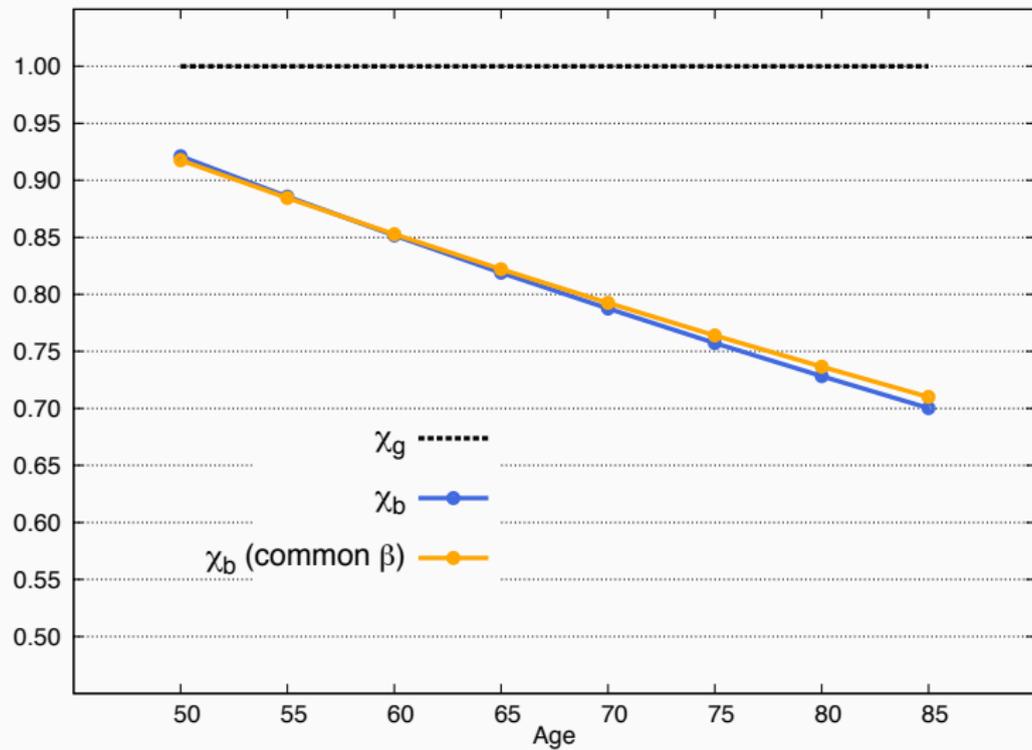
3. Uneducated are NOT more impatient: they have worse health outlook

# RESULTS

Men sample (with  $r = 2\%$ )

	$\beta$ edu specific		$\beta$ common	
$\sigma$	1.5		1.5	
$\beta^d$ (s.e.)	0.8861	(0.0175)	0.8720	(0.0064)
$\beta^h$ (s.e.)	0.8755	(0.0092)	0.8720	(0.0064)
$\beta^c$ (s.e.)	0.8634	(0.0100)	0.8720	(0.0064)
$\chi_b^0$ (s.e.)	0.9211	(0.0575)	0.9176	(0.0570)
$\chi_b^1$ (s.e.)	-0.0078	(0.0035)	-0.0073	(0.0035)
observations	15,432		15,432	
moment conditions	240		240	
parameters	5		3	
$\alpha_g$			0.066	
$\alpha_b$			0.048	

# RESULTS



# Preliminary Estimates: Health Technology

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- Health transitions:  $\forall \omega \in \tilde{\Omega}$

$$\tilde{\Gamma}(h_g | \omega) = \sum_{\eta} \pi_{\eta}^{ih} \left( \lambda_{0\eta}^{ieh} + \frac{\lambda_{1\eta}^{ieh}}{1 - \nu^{ih}} \frac{1}{M_{\omega}} \sum_j \mathbf{1}_{\omega_j = \omega} \tilde{x}_j^{1-\nu^{ih}} Pr[\eta | \omega_j, \tilde{x}_j] \right)$$

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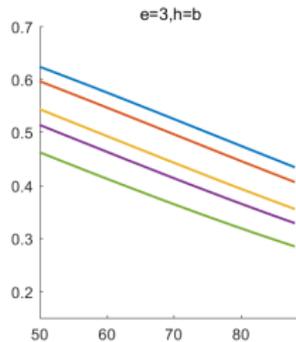
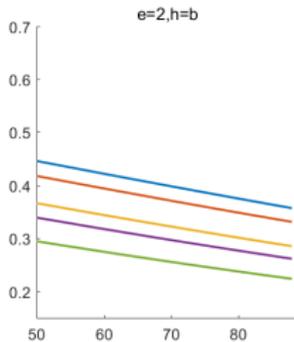
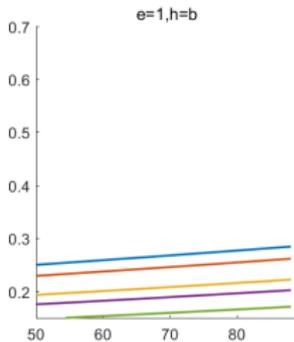
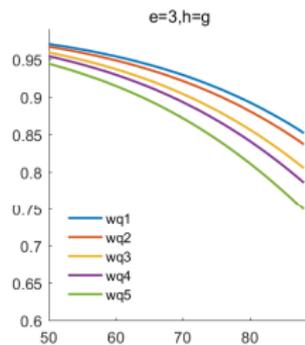
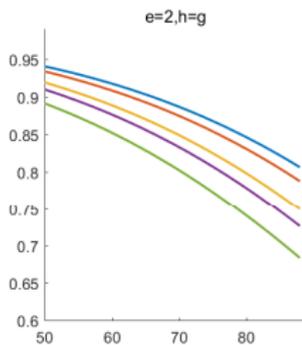
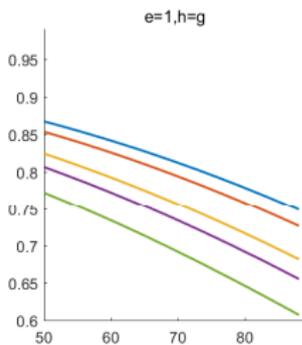
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- And we weight every individual observation by this probability

# THE PROBLEM

- Finally, need to estimate
  - the contingent health spending rule  $x(\omega, \eta)$
  - the probability distribution of health outlooks sock,  $\pi_{\eta_g}^{ih}$
  - the variance of the medical implementation error,  $\sigma_\epsilon^2$
- We identify all these objects through the observed health transitions  $\tilde{\varphi}(h_g|\omega, \tilde{x})$  as function of the state  $\omega$  and health spending  $\tilde{x}$

$$\underbrace{Pr[h_g|\omega, \tilde{x}]}_{\text{observed in the data}} = \Gamma^{ei}[h_g | h, \eta_g, \tilde{x}] \underbrace{Pr[\eta_g|\omega, \tilde{x}]}_{\text{posterior}} + \Gamma^{ei}[h_g | h, \eta_b, \tilde{x}] \underbrace{Pr[\eta_b|\omega, \tilde{x}]}_{\text{posterior}}$$

# AVERAGE HEALTH TRANSITIONS



## IMPLICATIONS FOR HEALTH TRANSITIONS

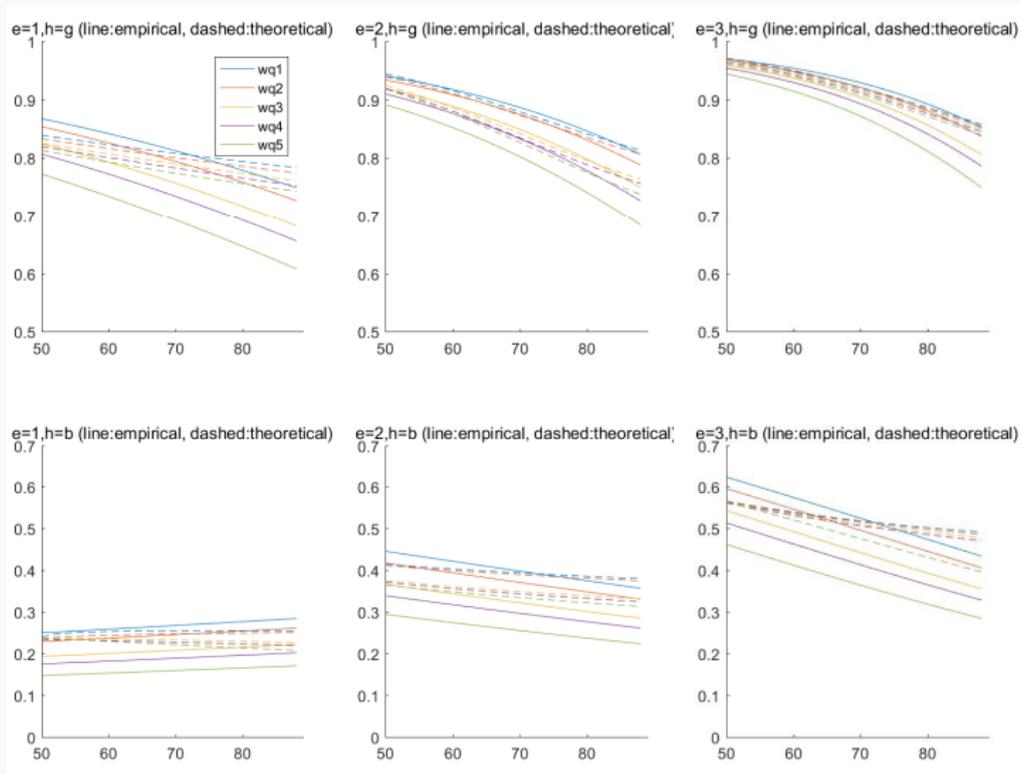
- We have preliminary estimates of health technology parameters

$$\theta_2 = \{\lambda_{0\eta}^{ieh}, \lambda_{1\eta}^{eh}, \nu^{ih}, \pi_{\eta}^{ih}, \sigma_{\epsilon}^2\}$$

- They generate health transitions that are consistent with
  - More educated have better transitions
  - Wealthier have better transitions
  - Older have worse transitions
- However, quantitatively, two problems remain
  - Worsening of health transitions with age milder than in the data (for some types)
  - Dispersion of transitions with wealth smaller than in the data

# PRELIMINARY ESTIMATES

## AVERAGE HEALTH TRANSITIONS



# Conclusions

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- So far not that different from calibrated simple version.

## REMAINING IMPORTANT ISSUES

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1. Estimation is closely dependant on U.S. features
  - Limited health insurance.
  - Not well defined role of Out of Pocket Expenditures. We are not sure if it means the same things across education groups.
2. Would love to use non U.S. data